

ON COMPUTATIONAL METHODS FOR SOLVING SOME NONLINEAR PARTIAL DIFFERENTIAL EQUATIONS

by

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FOR THE AWARD OF THE DEGREE OF
DOCTOR OF PHILOSOPHY*



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1992

... DEDICATED TO MY

GRANDFATHER

CERTIFICATE

This is to certify that the thesis entitled "ON COMPUTATIONAL METHODS FOR SOLVING SOME NONLINEAR PARTIAL DIFFERENTIAL EQUATIONS" which is being submitted by Mr. T.V.Singh for the award of DOCTOR OF PHILOSOPHY (MATHEMATICS) to the Indian Institute of Technology, Delhi, is a record of bonafide research work carried out by him under my guidance and supervision.

The thesis has reached the standard, fulfilling the requirements of the regulation relating to the degree. The results obtained in the thesis have not been submitted to any other University or Institute for the award of any degree or diploma.

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CONTENTS

	PAGE NO
SYNOPSIS	(i) - (vi)
CHAPTER-I: INTRODUCTION	1-16
CHAPTER-II: CUBIC SPLINE TECHNIQUE FOR SOLUTION OF BURGERS' EQUATION WITH A SEMI-LINEAR BOUNDARY CONDITION	17-32
INTRODUCTION	17
NUMERICAL METHOD	20
LOCAL TRUNCATION ERROR AND STABILITY OF THE METHOD	23
RESULTS AND DISCUSSION	25
CHAPTER-III: NUMERICAL TECHNIQUE FOR SOLVING BURGERS', MODIFIED BURGERS' AND CONVECTIVE REACTION DIFFUSION EQUATIONS	33-103
INTRODUCTION	33
SECTION-I: NUMERICAL METHOD	35
SECTION-II: NUMERICAL RESULTS FOR BURGERS' EQUATION	41
SECTION-III: MODIFIED BURGERS EQUATION NUMERICAL RESULTS AND DISCUSSION	44
SECTION IV: CONVECTIVE REACTION DIFFUSION EQUATION	47
RESULTS AND DISCUSSION	73
	74

CHAPTER-IV:	NUMERICAL SOLUTION OF REGULARIZED LONG WAVE EQUATION	104-122
	INTRODUCTION	104
	NUMERICAL METHOD	107
	LOCAL TRUNCATION ERROR AND STABILITY OF THE METHOD	109
	NUMERICAL EXAMPLES AND RESULTS	111
CHAPTER-V:	CUBIC SPLINE TECHNIQUE FOR THE SOLUTION OF QUASI-LINEAR HYPERBOLIC SYSTEM IN NON-CONSERVATIVE FORM	123-143
	INTRODUCTION	123
	SECTION-II: DIFFERENCE SCHEME	127
	SECTION-III: THE EQUATION OF MOTION AND PHYSICAL PROBLEM	131
	EQUATIONS IN NON-DIMENSIONAL FORM	133
	INITIAL AND BOUNDARY CONDITIONS	134
	NUMERICAL RESULTS	136
CHAPTER-VI:	ON CONVERGING CYLINDRICAL SHOCK PROBLEM IN RADIATION GAS DYNAMICS-NUMERICAL STUDY	144-165
	INTRODUCTION	144
	DIFFERENCE SCHEME	145
	EQUATION OF MOTION	148
	NUMERICAL RESULTS AND DISCUSSION	151
REFERENCES		166-175