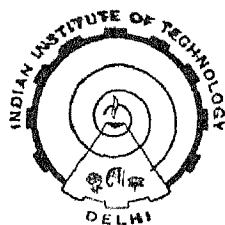


THEORY AND PHOTON STATISTICS OF A FREE-ELECTRON LASER

By
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