SOME STUDIES IN FACILITIES LOCATION PLANNING

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Some Studies In Facilities Location Planning

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DEDICATED TO

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The thesis entitled "Some Studies in Facilities Location Planning" submitted by Mr. Devinder Kumar Banwet to the Indian Institute of Technology, Delhi, for the award of the degree of Doctor of Philosophy, is a record of bonafide research work carried out by him. He has worked under my guidance and supervision and has fulfilled the requirements for the submission of this thesis, which has attained the standard required for a Ph.D. degree of this Institute. The results presented in this thesis have not been submitted elsewhere for the award of any degree or diploma.

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