

THE STRUCTURE OF UNIT GROUPS OF GROUP RINGS

by

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CERTIFICATE

This is to certify that the thesis entitled, "The Structure of Unit Groups of Group Rings" submitted by Mr. Vikas Bist to the Indian Institute of Technology, Delhi, for the award of the degree of Doctor of Philosophy in Mathematics, is a record of bonafide research work carried out by him under my supervision for the last five years. To the best of my knowledge it has reached the standard, fulfilling the requirements and regulations relating to the degree.

The results contained in this thesis have not been submitted, either in part or in full, to any University or Institute for the award of any degree or diploma.


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