

ON TOPOLOGIES OF SPACES OF SUBSETS
AND FUNCTION SPACES

S.B. Jalota

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CERTIFICATE

This is to certify that the thesis entitled "On topologies of spaces of subsets and function spaces" which is being submitted by Mrs. Shashi Bala Jalota for the award of Degree of Doctor of Philosophy (Mathematics) to the Indian Institute of Technology, Delhi, is a record of bonafied, research work. She has worked for the last four and a half years under my supervision and guidance.

The thesis has reached the standard fulfilling the requirements of the regulations relating to the degree. The results obtained in this thesis have not been submitted to any other University or Institute for the award of any degree or diploma.

S. N. Patnaik
(S.N. PATNAIK) 11/7/75
Department of Mathematics
Indian Institute of Technology
Hauz Khas, New Delhi-110029
India.

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(.SHASHI BALA JALOTA)

CONTENTS

	Page
CHAPTER 0	INTRODUCTION 1
CHAPTER I	ON TOPOLOGIES OF HYPERSETS..... 4
CHAPTER II	ON THE FUNCTION SPACE $C(X,Y)$ 26
CHAPTER III	ON CONTINUOUS RELATIONS..... 35
CHAPTER IV	ON TOPOLOGIES OF HYPERSETS AND FUNCTION SETS..... 55
CHAPTER V	ANOTHER PRODUCT TOPOLOGY AND FUNCTION SPACES 69
APPENDIX	ON SELECTION THEORY..... 83
REFERENCES	 91