

**ON THE CONTROL OF LINEAR TIME INVARIANT  
DISCRETE TIME MULTIVARIABLE SYSTEMS**

SUMANT VARSHNEY

**Department of Electrical Engineering**  
**INDIAN INSTITUTE OF TECHNOLOGY, DELHI**  
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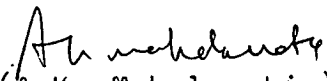
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New Delhi 110016

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C E R T I F I C A T E

This is to certify that the thesis entitled,  
'On the Control of Linear Time Invariant Discrete Time  
Multivariable Systems' being submitted by Sumant Varshney for  
the award of Doctor of Philosophy to the Indian Institute of  
Technology, Delhi is a record of bonafide research work he has  
carried out under our guidance and supervision. The  
results obtained in this thesis have not been submitted  
to any other university or institute for award of a degree  
or diploma.

  
(A.K. Mahalanabis)  
Professor

(K.K. Biswas)  
Asstt. Professor

Department of Electrical Engg,  
Indian Institute of Technology, Delhi,  
New Delhi-110016

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SUMANT VARSHNEY

# C O N T E N T S

		Page No.
	List of Abbreviations	... i
	List of Principal Symbols	... ii
	List of Figures	... vii
	List of Tables	... ix
	List of Publications	... x
	Abstract	... xi
CHAPTER-1	SCOPE OF THE WORK	
1.1	Introduction	... 1
1.2	Review of the Optimal Control Theory	... 2
1.3	Review of the Observer Design Theory	... 7
1.4	Review of the Deadbeat Control Theory	... 11
1.5	Scope of the Present Work	... 18
CHAPTER-2	OBSERVER DESIGN USING A SIMPLIFIED OBSERVABLE CANONICAL MODEL	
2.1	Introduction	... 23
2.2	Problem Statement	... 25
2.3	Derivation of the Simplified Observable Canonical State Model	... 27
2.4	Design of the Full Order Deadbeat Observer	... 31
	2.4.1 Computational Advantages of the Full Order Deadbeat Observer	... 35
2.5	Design of the Reduced Order Deadbeat Observer	... 36
	2.5.1 Computational Advantages of the Reduced Order Deadbeat Observer	... 40
2.6	Design of the Reduced Order Optimal Observer	... 42
	2.6.1 Computational Advantages of the Reduced Order Optimal Observer	... 44
2.7	Concluding Remarks	... 45

CHAPTER-3	CONTROLLER DESIGN USING SIMPLIFIED CONTROLLABLE AND OBSERVABLE CANONICAL MODELS		
3.1	Introduction	...	47
3.2	Problem Statements	...	49
3.3	Development of the Simplified Controllable Canonical Form	...	52
3.4	Development of a Computationally Simple Optimal State Feedback Control Algorithm.	...	54
3.5	Development of a Computationally Simple Observed State Feedback Control Algorithm	...	58
3.6	Development of a Computationally Simple PI Control Law	...	60
3.7	Development of a Deadbeat Controller for SRCC Form	...	65
	3.7.1 Computational Aspects	...	67
3.8	Concluding Remarks	...	69
CHAPTER-4	ON THE IDENTIFICATION AND CONTROL OF DISCRETE TIME SYSTEMS USING THE WA CANONICAL FORM		
4.1	Introduction	...	70
4.2	Problem Formulation	...	72
4.3	System Order Determination	...	75
4.4	Determination of the Elements of $\bar{A}$	...	80
4.5	Determination of the Elements of $\bar{B}$	...	82
4.6	Determination of the Elements of $K_y$	...	88
4.7	Results of a Simulation Study	...	91
4.8	Concluding Remarks	...	97

CHAPTER-5	CONTROLLER DESIGN FOR PRESCRIBED MODEL OUTPUTS	
5.1	Introduction	... 106
5.2	Problem Formulation	... 107
5.3	A New Interpretation of the Pole Position- ing Control Law	... 110
5.4	An Improved Modal Control for Systems with Given External Inputs	... 116
5.5	A Solution of the Regulator Design Problem	... 119
5.6	Concluding Remarks	... 122
CHAPTER-6	EXCITATION SYSTEM DESIGN FOR A SYNCHRONOUS GENERATOR	
6.1	Introduction	... 123
6.2	Development of the State Model	... 125
6.2.1	Description of the Nonlinear State Model	... 125
6.2.2	Determination of the Operating Point	... 130
6.2.3	Linearization of the State Model	... 132
6.2.4	Discretization of the State Model	... 134
6.3	Transformation of the State Model	... 137
6.4	Solution of the Control Problems	... 140
6.4.1	Optimal Control Solution	... 141
6.4.2	Deadbeat Control Solution	... 143
6.4.3	Improved Modal Control Solution	... 144
6.5	Results of a Simulation Study	... 146
6.6	Concluding Remarks	... 147

CHAPTER-7	SUMMARY AND SUGGESTIONS FOR FURTHER WORK		
7.1	Summary	...	152
7.2	Some suggestions for Further Work	...	155
7.2.1	Systems with time delay	...	155
7.2.2	Development of Decentralized Forms of Observers and Controllers	...	156
7.2.3	Development of Hierarchical Observer and Controller Structures	...	157
7.2.4	Solution of the Stochastic Optimal Control Problems	...	157
	REFERENCES	...	158