

**A THESIS ON
WAVE PROPAGATION THROUGH
NONLINEAR CONTINUOUS MEDIA**

By

**B.L. Juneja
Department of Mechanical Engineering
Indian Institute of Technology
New Delhi**

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Technology, New Delhi for the award
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C E R T I F I C A T E

This is to certify that the thesis entitled 'Wave Propagation Through Nonlinear Continuous Media', being submitted by Mr. B.L. Juneja to the Indian Institute of Technology, New Delhi, for the award of the Degree of Doctor of Philosophy in Mechanical Engineering, is a record of bonafide research work carried out by him. Mr. B.L. Juneja has worked under my guidance and supervision and has fulfilled the requirements for the submission of this thesis, which to my knowledge, has reached the requisite standard.

The results contained in this thesis have not been submitted in part or in full, to any other university or institute for the award of any degree or diploma.



(S.P. Luthra)
Professor and Head of Mech. Engg.,
Indian Institute of Technology,
Hauz Khas, New Delhi-29.

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Bhal Juneja
(B.L. Juneja)
Department of Mech. Engg.,
Indian Institute of Technology,
Hauz Khas, New Delhi-29.

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