

OPTIMIZATION OF CLUTTER REJECTION IN  
MTI RADAR SYSTEMS

KRISHNA ARORA

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Indian Institute of Technology, Delhi

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CERTIFICATE

This is to certify that the thesis, "Optimization of Clutter Rejection in MTI Radar Systems", which is being submitted by Krishna Arora for the award of the degree of Doctor of Philosophy of the Indian Institute of Technology, New Delhi, is a bonafide record of research work carried out by her over the last three years under my guidance and supervision.

The candidate has fulfilled the requirements of all the regulations relating to the degree. The results obtained in the thesis have not been submitted to any other university or institute for the award of a degree or diploma.

  
20.8.76

P. V. Indiresan

Department of Electrical Engineering

Indian Institute of Technology

New Delhi - 110029

INDIA

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