

STRENGTH AND DEFORMATIONAL RESPONSES OF SCHISTOSE ROCKS

By

MOHAMMAD-HOSSEIN NASSERI BEHRESTAGHI

A thesis Submitted

in fulfilment of the requirements for the degree of

DOCTOR OF PHILOSOPHY.



**Department Of Civil Engineering
INDIAN INSTITUTE OF TECHNOLOGY, DELHI**

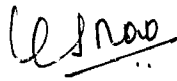
August 1992

*DEDICATED TO
MY
PARENTS*

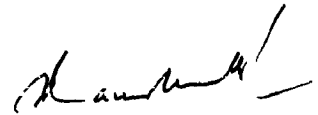
CERTIFICATE

This is to certify that the thesis entitled, "STRENGTH AND DEFORMATIONAL RESPONSES OF SCHISTOSE ROCKS" being submitted by Mr. Mohammad-Hossein Nasser Behrestaghi to the Indian Institute of Technology, Delhi, for the award of the degree of DOCTOR OF PHILOSOPHY is a record of the bonafied research work carried out by him. Mr. Nasser Behrestaghi has worked under our guidance for the submission of this thesis which to our knowledge has reached the required standard.

The thesis or any part thereof has not been submitted to any other University or Institution for the award of any degree or diploma.



Dr. K. Seshagiri Rao
Assistant Professor



Dr. T. Ramamurthy
Professor

Department of Civil Engineering
Indian Institute of Technology
New Delhi - 110016.

ACKNOWLEDGEMENT

It is a great pleasure to express my regards and profound sense of gratitude to my supervisors, Prof. T. Ramamurthy and Dr. K. Seshagiri Rao for their inspiring guidance, constant encouragement and immense help throughout the research programme. Without their understanding, untiring enthusiasm and great care this work would not have been possible.

Thanks are due to the staff of National Hydro-Electric Power Corporation working at New Delhi, Uri (Kashmir) and Jakhri (H.P.) for providing help in collection of rock samples from the project sites.

I take this opportunity to thank my friends and fellow scholars especially Dr. J. Singh, A. Katti, Anjani Kumar, F.H. Shamsher, M.P.S. Pradhan, N. Roy, S. Tripathi, K.M. Soni, S.Goel and A.Gupta for their help and suggestions at various stages of this work. Many happy moments and lively discussions have been shared with them.

The assistance rendered by the staff of Rock Mechanics Laboratory and Civil Engineering Workshop, X-ray diffraction and Scanning Electron Microscopy units is thankfully acknowledged.

I am deeply indebted to my family members especially my mother Mrs. Souroor Aghdas for her immense affection and encouragement at all stages of my study and research.

M. H. Nasser, B.

August, 1992

Mohammad-Hossein Nasser Behrestaghi
Entry No: 88RCE012

ABSTRACT

To understand the physico-mechanical behaviour of intrinsically anisotropic rocks, some investigators emphasized the necessity of conducting a number of triaxial test at a minimum of three orientations in order to predict the strength of anisotropic rocks at other orientations. Besides the need for predicting the strength, no precise attempt was made to understand and predict the behaviour of deformation modulus, stress-strain response, shear strength behaviour with minimum pre-evaluation experimental data. A non-linear strength criterion based on Mohr-Coulomb approach for intact and anisotropic intact rocks proposed by Ramamurthy and co-workers has shown better results as compared to a number of other available failure theories. With these findings in view, the present investigation is an attempt

- i) to evaluate the nature and engineering behaviour of the four varieties of schists with inherent anisotropies obtained from two Hydroelectrical project sites of Himalayan region, no such studies were carried out earlier on these rocks.
- ii) to compare the responses of these four schists with that of similar rocks studied earlier by other researchers.
- iii) to verify the applicability of the non-linear criterion proposed by Ramamurthy and co-workers for prediction of triaxial compressive strength of the schists with minimum pre-evaluation experimental data of two triaxial tests at $\beta = 90^\circ$ and uniaxial compressive tests of $\beta = 0, 30$ and 90° .
- iv) to propose an empirical criterion to predict the deformation modulus, stress-strain behaviour and shear strength behaviour at different confining pressures (σ_3), and orientations (β) of anisotropic schistose rocks.

In this study, the nature of Quartzitic, Chlorite, Quartz mica and Biotite schists was brought out using thin section, X-ray diffraction and Scanning Electron

Microscopic studies. The physical and strength properties were estimated using ISRM and Indian Standards (IS) test procedures.

Anisotropic strength behaviour of the schists was studied through testing of specimens with varying orientation (β) of schistosity with respect to the major principal stress, at an interval of 15° i.e. $0, 15, 30, 45, 60, 75$ and 90° . Triaxial tests were conducted at $\sigma_3 = 5, 15, 35, 50$ and 100 MPa at all the above orientations.

The schists under investigation have exhibited maximum compressive strength at $\beta = 90^\circ$ and the minimum between 30 to 45° showing "U-Shape" anisotropy curve similar to that of other schistose and metamorphic rocks. It has been observed that the anisotropic curve showing the variation of deformation modulus with β for anisotropic rocks is either "U-Shape" or "Irregular Shape". Two of the more competent schists i.e. Quartzitic and Chlorite schists fall under former class whereas other two less competent schists i.e. Quartz mica and Biotite schists can be categorised under later class.

The Brazilian and axial point load strengths increase at different rate for the four schists as β varies from, 0 to 90° (with respect to loading direction); whereas diametral point load strength behave contrary to this. Quartzitic schist exhibits maximum anisotropic ratio in terms of compression, tension and strain measurement. Biotite schist shows minimum anisotropic ratio in compression.

The strength prediction made on the basis of modified criterion proposed by Ramamurthy and co-workers shows a good agreement with the experimental data of schistose rocks for all orientations and confining pressures, using the triaxial test data only at $\beta = 90^\circ$ and uniaxial compressive strength at $0, 30$, and 90° orientations. The criterion slightly underpredicts the strength at 50 and 100 MPa of σ_3 for Quartzitic schist in the region $\beta < 45$ degrees. Using same strength criterion Ramamurthy and co-workers have shown a close agreement between the predicted strength and actual one for number of anisotropic rocks tested by numerous researchers. Keeping in view

the non-linear increment of deformation modulus at different confining pressures for different orientations (β), following empirical relationships have been proposed to predict the variation of deformation modulus at any orientation other than $\beta = 90^\circ$ and for complete range of confining pressure (σ_3):

$$\frac{E_{\beta 90}}{\sigma_3} = B_{e90} \left(\frac{\sigma_{c90}}{\sigma_3} \right)^{\alpha_{e90}} \quad (1)$$

Two more equations have been found to hold good to obtain the constant B_{ej} and α_{ej} at an orientation other than $\beta=90^\circ$. The uniaxial compressive strength at various orientations, σ_{cj} , is a scaling parameter for the non-dimensional parameters B_{ej} and α_{ej} ;

$$\frac{\alpha_{ej}}{\alpha_{e90}} = \left(\frac{\sigma_{cj}}{\sigma_{c90}} \right)^{1 - \alpha_{e90}} \quad (2)$$

$$\frac{B_{ej}}{B_{e90}} = \left(\frac{\alpha_{e90}}{\alpha_{ej}} \right)^{1 \text{ to } 3} \quad (3)$$

These two key equations enables to determine the values of α_{ej} and B_{ej} at various orientations through the values of α_{e90} and B_{e90} obtained with only two to three triaxial tests at $\beta = 90^\circ$, which is the same minimum test requirement proposed by Ramamurthy and co-workers to predict the strength behaviour of anisotropic rocks.

The analysis showed that the power in the proposed Eqn. (3) varies from 1 to 3 for schists in general and being 3 for Quartzitic and Chlorite schists, and 1.5 for Quartz mica and 1.1 for Biotite Schist.

Using predicted values for strength and deformation modulus values were obtained in the present study in a non-linear hyperbolic formula proposed by Kondner et al. It has been found that the predicted stress-strain curves agree well

with the experimental stress-strain curves of these schists.

To predict the shear strength behaviour of isotropic and anisotropic rocks with confining pressure, Mohr-Coulomb envelopes of more than 50 isotropic and 10 anisotropic rocks were constructed and analysed. Cohesive strength c , at each confining pressure (σ_3) was found and the value of c_0 i.e. cohesion corresponding to uniaxial compressive strength was evaluated. The following relationship has been proposed to predict c at any confining pressure in brittle range.

$$\frac{c}{\sigma_3} = B_c \left(\frac{c_0}{\sigma_3} \right)^{\alpha_c} \quad (4)$$

Based on the analysis of data obtained for isotropic rocks an average value of 0.6 has been suggested for α_c of all types of rocks. Using 0.6 as α_c in the above equation B_c has been found to be 1.5 for argillaceous, 1.8 for arenaceous, 2.1 and 3 for chemical and igneous rocks respectively.

By extending the above cited equation for predicting the value of c for anisotropic rocks, it has been proposed to replace the parameters c_0 , B_c and α_c with c_{oj} , B_{cj} and α_{cj} . These new parameters can be obtained through uniaxial compressive test and two triaxial compression tests at lower σ_3 at each of 0, 30 and 90° orientations respectively. The following equations are used to obtain the predicted c_{oj} , α_{cj} and B_{cj} for orientations other than 0, 30 and 90°.

$$c_{oj} = A_{oj} - B_{oj} \cos 2(\xi - \beta) \quad (5)$$

$$\alpha_{cj} = A_{cj} - B_{cj} \cos 2(\xi - \beta) \quad (6)$$

$$B_{cj} = A_{cj} - B_{cj} \cos 2(\xi - \beta) \quad (7)$$

Through the predicted values of strength and c at any confining pressure the value of angle of internal friction (ϕ) can be determined.

Predicted value of c at different σ_3 and β for a number of anisotropic rocks, match well with the observed values.

CONTENT		<u>Page No.</u>
Acknowledgement		
Abstract		i
List of Table		v
List of Figures		xii
List of Notations		xxiv
CHAPTER 1 INTRODUCTION		1
1.1 Organization of the Thesis		4
CHAPTER 2 LITERATURE REVIEW		5
2.1 Factors Influencing the Strength of Rocks		5
2.1.1 Geological Factors		5
2.1.2 Lithological Factors		6
2.1.2.1 Texture		6
2.1.2.1.1 Grain Size of Metamorphic Minerals		9
2.1.2.1.2 Metamorphic Differentiation		9
2.1.2.2 Mineral Composition		9
2.1.3 Physical Properties		10
2.1.4 Mechanical Factors		13
2.1.5 Environmental Factors		15
2.2 Tensile Strength		16
2.2.1 Direct Tensile Test		16
2.2.2 Indirect Tensile Test		18
2.2.2.1 Brazilian Tests		18
2.2.2.2 Point Load Test		23
2.3 Uniaxial Compressive Strength		23
2.4 Deformational Behaviour of Anisotropic Rocks		25

2.5	Stress-Strain Relation	28
2.6	Types of Anisotropy	33
2.7	Triaxial Strength	40
2.7.1	Behaviour of Anisotropic Rocks in Axi-symmetric Triaxial Condition	44
2.8	Effect of Confining Pressure on Anisotropy	48
2.9	Strength Criteria for Isotropic Rocks	52
2.10	Strength Criteria for Anisotropic Rocks	60
2.10.1	Single Plane of Weakness Theory	60
2.10.2	Variable Co-efficient of Friction and Cohesive Strength Theory	61
2.10.3	Walsh-Brace Theory	62
2.10.4	Modified Variable Cohesive Strength Theory	63
2.10.5	Hoek and Brown Theory	63
2.10.6	Non-Linear Criterion for Anisotropic Rocks	65
2.11	Brittle Fracture of Rocks	67
2.12	Ductile Behaviour of Rocks	75
2.13	Conclusion	79
CHAPTER 3	EXPERIMENTAL INVESTIGATION	81
3.1	Rocks Tested	81
3.1.1	Quartzitic and Chlorite Schists	81
3.1.2	Quartz mica and Biotite Schists	83
3.2	Test Programme	84
3.3	Petrographic and Petro-fabric Analysis	86
3.3.1	Quartzitic Schist	86
3.3.2	Chlorite Schist	89
3.3.3	Quartz Mica Schist	89
3.3.4	Biotite Schist	94

3.4	Physical Properties	100
3.4.1	Density, Porosity and Water Absorption	100
3.5	Specimen Preparation	102
3.6	Geotechnical Behaviour	103
3.6.1	Unconfined Compression Test	103
3.6.2	Brazilian Test	107
3.6.3	Point Load Test	107
3.6.4	Triaxial Compression Test	107
3.6.4.1	High Pressure Triaxial Cell	112
3.6.4.2	Loading and Load Monitoring System	112
3.6.4.3	Deformation Measuring System	116
3.7	Permeability Test	116
CHAPTER 4	INDEX PROPERTIES AND PERMEABILITY	121
4.1	Tensile Strength	121
4.1.1	Brazilian Strength (σ_b)	121
4.1.2	Point Load Strength	124
4.1.2.1	Axial Point Load Strength (σ_{tpa})	124
4.1.2.2	Diametral Point Load Strength (σ_{tpd})	124
4.2	Uniaxial Compressive Strength (σ_c)	128
4.3	Deformation Behaviour	135
4.3.1	The Stress-Strain Curves	135
4.3.2	Deformation Modulus	135
4.3.3	Intact Rock Classification	139
4.4	Permeability	141
4.5	Anisotropy	145
4.5.1	Compressive Strength Anisotropy	145
4.5.2	Tensile Strength Anisotropy	147

	4.5.3 Deformation Modulus Anisotropy	147
	4.5.4 Strain Ratio Anisotropy	147
	4.6 Failure Mechanism in Uniaxial Compression Test	150
CHAPTER 5	STRENGTH AND DEFORMATION EVALUATION AND PREDICTION	154
	5.1 Strength Prediction in Unconfined State	154
	5.2 Strength Behaviour in Triaxial Condition	155
	5.2.1 Effect of Confinement on Anisotropy	162
	5.2.2 Prediction of Failure Strength	165
	5.3 Deformation Behaviour in Confined State	185
	5.3.1 Effect of Confinement on Deformation Modulus	189
	5.3.2 Prediction of Deformation Modulus	193
	5.3.2.1 Basis for the Prediction	195
	5.3.3 Strain Ratio Under Triaxial State	196
	5.4 Stress-Strain Curves Under Triaxial Condition	207
	5.4.1 Effect of Confinement on Axial and Diametral Strain	218
	5.4.1.1 Axial Strain (ϵ_a)	218
	5.4.1.2 Diametral Strain (ϵ_d)	223
	5.4.2 Prediction of Stress-Strain Curve under Triaxial Condition	223
	5.4.2.1 Prediction of R_f Value	239
	5.5 Shear Strength Behaviour	239
	5.5.1 Shear Strength Parameters for Isotropic Rocks	239
	5.5.1.1 Indiana Limestone	251
	5.5.2 Shear Strength Parameter for Anisotropic Rocks	251
	5.5.3 Effect of Confinement on Shear Strength Parameter	254

5.5.4 Prediction of Shear Strength Parameters	265
5.5.4.1 Basis for the Proposition	268
5.6 Failure Pattern in Confined State	271
5.6.1 Macro-Fracture Pattern	290
5.6.2 Micro-Fracture Pattern	295
5.7 Brittle-Ductile Transition	301
CHAPTER 6 SUMMARY AND CONCLUSIONS	309
6.1 Nature and Index Properties	309
6.1.1 Petrography and Petrofabric Analysis	309
6.2 Index Properties	311
6.3 Anisotropy	312
6.4 Strength and Deformation Behaviour in Confined State	313
6.5 Prediction of Strength in Confined State	313
6.6 Prediction of Deformation Modulus in Confined State	313
6.7 Stress-Strain Response	315
6.8 Prediction of Stress-Strain Curves	315
6.9 Shear Strength Parameters	316
6.9.1 Isotropic Rocks	316
6.9.2 Anisotropic Rocks	316
6.10 Failure Pattern in Unconfined State	318
6.11 Failure Pattern in Confined State	318
6.12 Brittle-Ductile Transition	319
REFERENCES	321
APPENDIX	331