

NON-GENUINE ADJUNCTIONS

By
Arun Kumar Srivastava
Department of Mathematics
Indian Institute of Technology
New Delhi

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(Arun Kumar Srivastava)

CERTIFICATE

This is to certify that the thesis entitled "Non-genuine Adjunctions" which is being submitted by Mr. Arun Kumar Srivastava for the award of Doctor of Philosophy (Mathematics) to the Indian Institute of Technology, Delhi, is a record of bonafide research work. He has worked for the last three years under my guidance and supervision.

The thesis has reached the standard fulfilling the requirements of the regulations relating to the degree. The results in this thesis have not been submitted to any other University or Institute for the award of any degree or diploma.

Wagish Shukla

(Wagish Shukla)
Department of Mathematics
Indian Institute of Technology
Hauz Khas, New Delhi-110029

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