

STUDIES IN SIGNAL THEORY

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Thesis submitted in partial fulfilment of the requirements
for the degree of Doctor of Philosophy
in Electrical Engineering

to

Indian Institute of Technology, Delhi

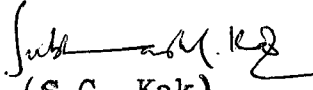
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ACKNOWLEDGEMENTS

The author is highly grateful to Professor P.V.Indiresan without whose constant encouragement and guidance this work would not have been possible.

He is also thankful to Dr. A.C. Kak and Mr. A.Paul Raj for useful discussions.

Thanks are due to Mr. T.N.Gupta for expert typing of the manuscript.


(S.C. Kak)

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