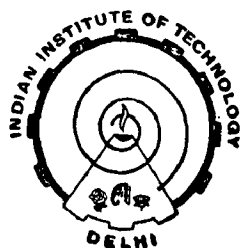


RANKING AND SELECTION IN THE METHOD OF PAIRED COMPARISON

By
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Thesis Submitted to the
Indian Institute of Technology, New Delhi
for the award of the Degree of
DOCTOR OF PHILOSOPHY



Department of Mathematics
INDIAN INSTITUTE OF TECHNOLOGY, DELHI
OCTOBER 1983

DEDICATED

TO

MY PARENTS

CERTIFICATE

This is to certify that the thesis entitled "RANKING AND SELECTION IN THE METHOD OF PAIRED COMPARISON" being submitted by K.S. SCARIAH to the Indian Institute of Technology, Delhi for the award of Doctor of Philosophy in Statistics is a record of bonafide research work carried out by him. Shri K.S. SCARIAH has worked under our guidance and supervision and has fulfilled the requirements for the submission of this thesis, which to the best of our knowledge, has reached the requisite standard.

The results contained in this thesis have not been submitted in part or in full, to any other University or Institute for the award of any degree or diploma.



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K S. Scariah

(K.S. SCARIAH)

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