

OPTIMALITY CRITERIA AND DUALITY IN MINIMAX PROGRAMMING

By

VIVEKA KUMAR (nee) KUDESIA
Department of Mathematics

Submitted

in fulfilment of the requirements
for the degree of

DOCTOR OF PHILOSOPHY



to the

INDIAN INSTITUTE OF TECHNOLOGY, DELHI

HAUZ KHAS, NEW DELHI-110016

INDIA

JULY, 1995

Dedicated to the fond memory of

my father Shri Krishna Kant Kudesia

CERTIFICATE

This is to certify that the thesis entitled OPTIMALITY CRITERIA AND DUALITY IN MINIMAX PROGRAMMING which is being submitted by Mrs. Viveka Kumar ne. Kudesia for the award of the degree, DOCTOR OF PHILOSOPHY IN MATHEMATICS, to the Indian Institute of Technology Delhi, is a bonafide record of research work done under my guidance and supervision.

The thesis has reached the standards fulfilling the requirements of the regulations relating to the degree. The results obtained in this thesis have not been submitted to any other University or Institute for the award of any degree or diploma.

Department of Mathematics
Indian Institute of Technology
Hauz Khas, New Delhi-110 016



(SURESH CHANDRA)

ACKNOWLEDGMENTS

It is my privilege to express my profound sense of gratitude to my research supervisor Prof. Suresh Chandra for his invaluable guidance and constant encouragement throughout the course of my research work.

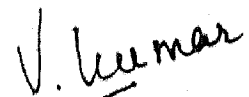
I am thankful to Prof. C.R. Bector, University of Manitoba (Canada) for many useful discussions during his visits to the Department of Mathematics, I.I.T. Delhi.

My sincere thanks to Prof. K. N. Mehta, Head of the Mathematics Department for his support and goodwill. I am grateful to Prof. N.S. Kambo and Prof. M.C. Puri for encouragement and interest in my work.

I cannot forget to remember and record my gratitude to Prof. (Mrs.) Pramila Srivastava and Prof. K. K. Azad, University of Allahabad, who initiated and motivated me for research work.

It is real pleasure to acknowledge the endurance and affection of my parents, aunt, brother and sister. I would also like to express my deep sense of indebtedness to my husband, Nagendra, for his patience, understanding and valuable suggestions. To my son, Praketa, I owe more than I can express.

Lastly I take this opportunity to thank my research colleagues for various help they rendered at various stages of my stay at I.I.T., Delhi.



VIVEKA KUMAR

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