

**GENERALISED CIRCUIT MODEL FOR THE ANALYSIS OF  
THREE PHASE INDUCTION MOTOR FED FROM SINGLE PHASE  
SUPPLY USING STATIC PHASE CONVERTERS**

by  
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DEDICATED  
TO  
MY PARENTS  
AND  
SISTER VASUMATI

CERTIFICATE

Certified that the thesis entitled 'Generalised Circuit Model for the Analysis of Three Phase Induction Motor Fed From Single Phase Supply Using Static Phase Converters', which is being submitted by Mr. N.C. Sonpal, in partial fulfilment for the award of the Degree of Doctor of Philosophy in Electrical Engineering of the Indian Institute of Technology, Delhi, is a record of student's own work carried out by him under our joint supervision and guidance. The matter embodied in this thesis has not been submitted for the award of any other Degree or Diploma.

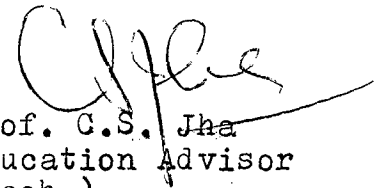


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