

A THESIS ON
A GENERALIZED ONE DIMENSIONAL RANDOM WALK-ASSOCIATED
CONVOLUTION IDENTITIES AND INVERSE SERIES RELATIONS

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C E R T I F I C A T E

This is to certify that the thesis entitled
'A Generalized One Dimensional Random Walk-Associated
Convolution Identities and Inverse Series Relations'
which is being submitted by Mr. B.R. Handa for the
award of Doctor of Philosophy (Mathematics) to the
Indian Institute of Technology, Delhi, is a record of
bonafide research work. He has been working since
September 1966 under my guidance and supervision.

The thesis has reached the standard fulfilling
the requirements of the regulations relating to the
degree. The results obtained in this thesis have not
been submitted to any other University or Institute for
the award of any degree or diploma.

S. G. Mohanty Oct 1/6
(S. G. Mohanty)

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