

# **VIBRATION ANALYSIS OF HIGH PRESSURE STAGE PACKETTED ROTOR BLADES**

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**Submitted**  
In Fulfilment of the Requirements for the Degree  
of  
**DOCTOR OF PHILOSOPHY**

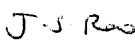


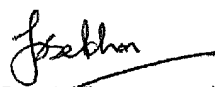
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JULY 1984**


CERTIFICATE

This is to certify that the thesis entitled, "Vibration Analysis of High Pressure Stage Packetted Rotor Blades" being submitted by Mr. Ahmad Cameron to the Department of Applied Mechanics, Indian Institute of Technology, Delhi, for the award of the Degree of Doctor of Philosophy is a record of bonafide research work carried out by him. He has worked under our supervision and guidance, and has fulfilled the requirement for the submission of this thesis, which in our opinion has reached the requisite standard.

The results contained in this work has not been submitted in part or in full, to any other University or Institute for the award of any degree or diploma.

  
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## ACKNOWLEDGEMENT

I wish to thank my supervisors Prof. J.S. Rao, Dr. G.S. Sekhon and Dr. Y. Nath whose guidance and supervision made it possible to complete this work. In this long period, above all, they infused the zeal when it was required most.

I am grateful to each one of my friends and associates who helped me directly or indirectly during this course of study. This prolonged association with them and with the Institute witnessed a queer combination of love with abuses; joy with depression; learning with rusting; knowledge with wickedness; arguments with poetry and crusades with reversals. It was simply beautiful.

I would also like to thank M/s Madhu, H.L. Sharma, Gamdur Singh and Rajbir members of the staff, Vibrations and Instrumentation Research Laboratory, I.I.T., Delhi, for extending their help in conducting the experimental work successfully and Mr. Bhatia for taking pains in typing the manuscript.

Lastly, I am indebted to my family members who had to bear all through this period.

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