

A THESIS ON  
FINITE UNIAXIAL COMPRESSION UNDER STATIC  
LOADING

BY

Kharag Singh Shishodia  
Department of Applied Mechanics  
Indian Institute of Technology,  
Delhi

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Technology, Delhi, for the award of  
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CERTIFICATE

This is to certify that the thesis entitled  
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by Shri Kharag Singh Shishodia has been prepared  
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The research report and results presented in the thesis  
have not been submitted for any other degree in any  
university.



(G.S. Sakhon)

Assistant Professor,  
Applied Mechanics Department,  
Indian Institute of Technology,  
Delhi.



(B. Karunes)

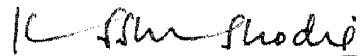
Professor of Applied Mechanics,  
Indian Institute of Technology,  
Delhi.

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CONTENTS

|             |   |    |
|-------------|---|----|
|             | NOTATIONS   | iv |
| CHAPTER-I   | INTRODUCTION  | 1  |
| 1.1         | The Compression Problem                                     | 1  |
| 1.2         | Review of the previous analytical work                      | 3  |
| 1.3         | Review of the past experimental studies                     | 7  |
| 1.4         | Deductions from the review                                  | 10 |
| 1.5         | The present work  | 11 |
| 1.6         | Major observations  | 15 |
| CHAPTER-II  | FORMULATION OF THE PROBLEM AND GOVERNING EQUATIONS          | 17 |
| 2.1         | Description of the overall compression problem              | 17 |
| 2.2         | Description of the incremental compression problem          | 20 |
| 2.3         | Governing Equations for the incremental compression problem | 21 |
| CHAPTER-III | COMPUTATIONAL PROCEDURE                                     | 35 |
| 3.1         | Nature of the Governing equations                           | 35 |
| 3.2         | Computational procedure                                     | 35 |
| 3.3         | Accuracy and efficiency of computations                     | 47 |
| 3.4         | Preliminary validity checks on computed results             | 50 |

|            |   |    |
|------------|---|----|
| CHAPTER-IV | EXPERIMENTAL VERIFICATION OF THEORETICAL RESULTS                                      | 52 |
| 4.1        | The plan of Experimentation   | 52 |
| 4.2        | Procedure for the compression tests   | 53 |
| 4.3        | Experimental determination of material parameters                                     | 56 |
| 4.4        | Determination of coefficient of friction  | 60 |
| 4.5        | Comparison of Theoretical and Experimental results                                    | 62 |
| CHAPTER-V  | ANALYSIS OF THEORETICAL RESULTS   | 68 |
| 5.1        | Range of parameter for theoretical computations                                       | 68 |
| 5.2        | The characteristic distributions of the components of displacement, strain and stress | 68 |
| 5.3        | Distribution of effective stress and effective strain during compression              | 72 |
| 5.4        | Rationale of the nature and progress of compressive deformation                       | 75 |
| 5.5        | Effect of the parameters of the compression   | 81 |
| CHAPTER-VI | CONCLUDING REMARKS  | 88 |
| 6.1        | Genesis of the present study  | 88 |
| 6.2        | Progress of the work  | 88 |
| 6.3.       | Conclusions from the present work   | 90 |
| 6.4        | Suggestions for further work  | 92 |

|            |  |     |
|------------|--|-----|
| REFERENCES |  | 97  |
| APPENDIX-A | Transformation of equation of equilibrium in the radial direction in terms of incremental displacements        | 103 |
| APPENDIX-B | Transformation of the equation of equilibrium in the axial direction in terms of the incremental displacements | 111 |
| APPENDIX-C | Values of stress components in elastic range   | 118 |
| APPENDIX-D | Composition of electrolytic copper and low carbon steel  | 122 |