

**ON SOME ASPECTS OF  
OPTIMAL DISTRIBUTION SYSTEM PLANNING**

**A Thesis Submitted  
in Partial Fulfilment of the Requirements  
for the Degree of  
DOCTOR OF PHILOSOPHY**

**By**

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DEDICATED

TO

MY PARENTS

## CERTIFICATE

Certified that this work, 'On Some Aspects of Optimal Distribution System Planning', by Mr. Murugesan Ponnaivaikko has been carried out under our supervision and that this work has not been submitted elsewhere for a degree.



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## ABSTRACT

This thesis presents the results of the investigation on certain important aspects of optimal distribution system planning.

The problems considered are

- (a) distribution system parameter optimization,
- (b) optimal grading of conductor cross-sections for radial distribution feeders,
- (c) optimal sizing and siting of substations and network routing for a specific distribution system, and
- (d) optimal choice of fixed and/or switched on-line shunt capacitors along the radial distributors.

The main contributions of this investigation include

- (i) development of new concepts for modelling non-uniform loading in a distribution system,
- (ii) formulation of mathematical models considering growth factors for the various distribution system components, costs and problems,
- (iii) development of simple solution methods and procedures for solving the above problems subject to voltage drop/rise and network constraints, and
- (iv) development of simple planning aids for the practicing engineers.

The effect of growth factors such as growth in load factor and increase in cost of energy with time is incorporated in the

parameter optimization problem and a two level optimization technique is suggested for its solution. Simple planning aids in the form of nomograms are also developed for obtaining the feeder power losses, substation feed-areas and the feeder main lengths, to serve the practicing engineer as ready reckoners for his regular system expansion planning. The effect of a variation in the system cost components on the optimal distribution system parameters is demonstrated through the results of a system study using the proposed method. The conductor gradation problem is studied considering the effect of growth factors and the feeder voltage drop constraint using two direct search solution techniques, namely the dynamic programming (DP) and the method of local variations (MLV). Results are presented to clearly demonstrate the effects of growth factors on optimal conductor grading. Nomograms are also developed for obtaining readily the optimal conductor gradation of a given radial distribution feeder. The optimal sizing and siting of substations and network routing problem is formulated as a Quadratic Mixed Integer Programming (QMIP) problem. The solution to this QMIP problem is obtained in two stages using, in the first stage, the procedure developed by Wolfe for solving quadratic programming problems. In the second stage, an integerization procedure is adopted for obtaining the integer values of the integer variables associated with the substation locations and feeder branch elements. The optimization procedure suggested, here, is very effective in obtaining the optimal network solutions without the need for linearizing the non-linear loss cost functions. The optimal capacitor allocation

problem is studied considering the effect of growth factors and the constraint on the nodal voltage rise during off-peak hours due to over-compensation of fixed shunt capacitor banks along the feeder mains. The solution to the problem is obtained using the DP and the MLV. The effect of growth factors and the influence of the cost of capacity release in the feeders on the optimal allocation of fixed and switched shunt capacitors are clearly demonstrated through the results of the sample systems studied.

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